#### APPENDIX A

### % BEGINNING OF PSEUDO CODE

% compute scale factor A, and time constants a, b from physical system parameters

A = Vmax \* Kt / (Re \* Rm + Kt \* Kb) \* 1 \* k;

10 p1 =  $1/\text{Jm/Ie} * (-\text{Ie} * \text{Rm} - \text{Re} * \text{Jm} + \text{sqrt}(\text{Ie}^2 * \text{Rm}^2 - 2 * \text{Re} * \text{Rm} * \text{Ie} * \text{Jm} + \text{Re}^2 * \text{Jm}^2 - 4 * \text{Kt} * \text{Kb} * \text{Ie} * \text{Jm})) / 2;$ 

 $p2 = 1/Jm/Ie * (-Ie * Rm - Re * Jm - sqrt(Ie^2 * Rm^2 - 2 * Re * Rm * Ie * Jm + Re^2 * Jm^2 - 4 * Kt * Kb * Ie * Jm)) / 2;$ 

15 a = max(-p1,-p2)b = min(-p1,-p2)

% make initial guesses for step durations

20 et1 = 1; et2 = .005; et3 = 1;

% set maximum iteration count

25 Nmax = 1000;

for j = 1:Nmax

% save old values of step time intervals

et3old = et3;

```
et2old = et2;
              et1old = et1;
              % iterate for switch times using fixed voltage level Vmax
 5
              et3 = -log(1.0 / 2.0 - exp(-et1 * a) / 2 + exp(-et2 * a)) / a;
              et2 = \frac{1}{b} * \log(2.0) + 3 * et3 - \frac{1}{b} * \log(2 * \exp(\frac{1}{A} * b * X) * \exp(et3)
                      * b) - sqrt(4.0) * sqrt(exp(1/A * b * X)) * exp(et3 * b) *
                      sqrt(exp(1/A * b * X) + exp(et3 * b)^2 - 2 * exp(et3 * b)));
              et1 = -(-2 * A * et2 + 2 * A * et3 - X) / A;
10
              if norm([et3old - et3 et2old - et2 et1old - et1], inf) <= eps * 2
                      break
              end
15
              if j==Nmax
                              error(['error - failure to converge after ', num2str(Nmax),'
                      iterations'])
              end
              end
20
              % round up pulse duration to nearest sample interval,
              % convert to intervals between steps to make sure that voltage
              % requirements will not increase (beyond Vmax).
25
              dt1=ceil((et1 - et2) / dt) * dt;
              dt2=ceil((et2 - et3) / dt) * dt;
              dt3=ceil((et3) / dt) * dt;
              et123 = [et1, et2, et3]
30
              % convert back to total step duration.
```

et1 = 
$$dt1 + dt2 + dt3$$
;  
et2 =  $dt2 + dt3$ ;  
et3 =  $dt3$ ;

% In the following, the original constraints equations involving XF1, XF2, was and XF3 have been modified to include a variable voltage level applied at

% each step (instead of the fixed maximum (+/-) Vmax).

10 % The original equations for XF1, XF2, and XF3 follow:

% 
$$XF_1(t_{end}) = V_0F_1(t_{tend} - t_0) - 2V_0F_1(t_{end} - t_1) + 2V_0F_1(t_{end} - t_2)$$

% 
$$XF_2(t_{end}) = V_0F_2(t_{tend} - t_0) - 2V_0F_2(t_{end} - t_1) + 2V_0F_1(t_{end} - t_2)$$

% 
$$XF_3(t_{end}) = V_0F_3(t_{tend} - t_0) - 2V_0F_2(t_{end} - t_1) + 2V_0F_1(t_{end} - t_2)$$

15 % And the modified equation including adjustable relative levels of voltage

% L1, L2 and L3 are:

% 
$$XF_1(t_{end}) = L_1V_0F_1(t_{tend} - t_0) - L_2V_0F_1(t_{end} - t_1) + L_3V_0F_1(t_{end} - t_2)$$

% 
$$XF_2(t_{end}) = L_1V_0F_2(t_{tend} - t_0) - L_2V_0F_2(t_{end} - t_1) + L_3V_0F_1(t_{end} - t_2)$$

20 
$$XF_3(t_{end}) = L_1V_0F_3(t_{tend} - t_0) - L_2V_0F_2(t_{end} - t_1) + L_3V_0F_1(t_{end} - t_2)$$

% And the corresponding constraint equations are:

$$\%$$
  $XF_1(t_{end}) = Finalpos$ 

$$% XF_2(t_{end}) = 0$$

25 % 
$$XF_3(t_{end}) = 0$$

% Where all of the times indicated have discrete values, e.g. corresponding to

% the controller update rate.

30

10

25

% It should be noted that after the digital switch times are fixed, the constraint

% equations derived from the equations above form a linear set of equations in

5 % the unknown relative voltage levels L1, L2 and L3 and any standard linear

% method can be used to solve for the relative voltage levels. In the equations

% for (L1, L2 and L3) that follow, the solution was obtained by algebraic % means (and are not particularly compact.)

% compute new relative voltage step levels

% L1, L2 and L3 are nominally assigned to "1", "-2" and "+2", respectively

15 s1 = 
$$X * (exp(-et3 * b) * exp(-et2 * a) + exp(-et3 * a) + exp(-et2 * b) - exp(-et2 * b) * exp(-et3 * a) - exp(-et3 * a) - exp(-et3 * b));$$

L1 = s1 \* s2;

```
\exp(-\text{et2} * a) + \exp(-\text{et3} * a) * \text{et1} + \exp(-\text{et2} * b) * \text{et1}
                             \exp(-\text{et2} * b) * \text{et1} * \exp(-\text{et3} * a) - \text{et3} * \exp(-\text{et1} * b) *
                             exp(-et2 * a) - exp(-et2 * a) * et1 - exp(-et3 * b) * et1 - exp(-et3 *
                   b) * et2 * exp(-et1 * a) + et3 * exp(-et1 * b) + et2 * exp(-et1 * a) +
  5
                             \exp(-et3 *b) * et2 + et3 * \exp(-et2 *a)) * X;
                   (\exp(-et2 * b) * \exp(-et1 * a) - \exp(-et1 * a) - \exp(-et2 * b) -
        s2 =
                             \exp(-\text{et1} * b) * \exp(-\text{et2} * a) + \exp(-\text{et1} * b) + \exp(-\text{et2} * a)) / A;
                   L3 = s1*s2;
10
        s1 = \exp(-et1 * a) - \exp(-et3 * a) + \exp(-et3 * b) - \exp(-et1 * b) -
                             \exp(-\text{et3 * b}) * \exp(-\text{et1 * a}) + \exp(-\text{et1 * b}) * \exp(-\text{et3 * a});
        s2 = X/(et2 * exp(-et1 * b) * exp(-et3 * a) + exp(-et2 * b) * et3 *
                             \exp(-\text{et1} * a) - \text{et2} * \exp(-\text{et3} * a) - \text{et2} * \exp(-\text{et1} * b) - \text{et3} *
                             \exp(-\text{et1} * a) - \exp(-\text{et2} * b) * \text{et3} + \exp(-\text{et3} * b) * \text{et1} * \exp(-\text{et2} * a)
                   a) + \exp(-\text{et3} * \text{a}) * \text{et1} + \exp(-\text{et2} * \text{b}) * \text{et1} - \exp(-\text{et2} * \text{b}) * \text{et1} * \exp(-\text{et2} * \text{b})
15
                   et3 * a) - et3 * exp(-et1 * b) * exp(-et2 * a) - exp(-et2 * a) * et1-exp(-et3 *
                   b) * et1 - \exp(-\text{et3} * \text{b}) * \text{et2} * \exp(-\text{et1} * \text{a}) + \text{et3} *
                             \exp(-\text{et1} * b) + \text{et2} * \exp(-\text{et1} * a) + \exp(-\text{et3} * b) * \text{et2} + \text{et3} *
                             \exp(-\text{et}2 * a)) / A;
20
                   L2 = s1 * s2;
                   % convert accumulated voltage steps to sequential voltage level
                   V1 = Vmax * (L1);
25
                   V2 = Vmax * (L1 + L2);
                   V3 = Vmax * (L1 + L2 + L3);
```

% END OF PSEUDO CODE

15

#### APPENDIX B

AREA .. SUM(I,A(I)) = E = 0;

VELOCITY(VINDX) .. VEL(VINDX) =E= VSCALE

- 5 SUM(I\$(ORD(I) LE ORD(VINDX)), A(I));
  - $\begin{aligned} & \texttt{POSITION} \ .. \ & \texttt{SUM(I,VEL(I))} = \texttt{E=FINALPOS} * \ & \texttt{SCALEFACT;} \\ & \texttt{VLIMITP(I)} \ .. \ & \texttt{SUM(VINDX\$(ORD(VINDX) LE ORD(I)),A(I-I)} \end{aligned}$

(ORD(VINDX)+1))\*(VOLTS(VINDX)+KBACK\*VSCALE))

=L= VOLTLIM;

- VLIMITN(I) .. SUM(VINDX\$(ORD(VINDX) LE ORD(I)), A(I-(ORD(VINDX)+1))\*(VOLTS(VINDX)+KBACK\*VSCALE))

  =G= -VOLTLIM
  - % A(I) are the current commands at time T(I) spaced equally at time DT.
  - % VOLTS(VINDX) is a table of voltages representing the unit pulse response to
  - % a unit output in current command. VOLTLIM is the voltage limit at saturation.

## APPENDIX C

	GOALPOS SUM(I,A(I)*MODELAA*DT) =E=FINALPOS;
	MODE1(ILAST) SUM(I,-A(I)*MODELAA*MODELb/(MODELb-
5	MODELa)*(EXP(-MODELa*(T(ILAST)+DT-T(I)))
	-EXP(-MODELa* $(T(ILAST)-T(I))))) = E = 0.0;$
	MODE2(ILAST) SUM(I,A(I)*MODELAA*MODELa/(MODELb-
	MODELa)*(EXP(-MODELb*(T(ILAST)+DT-T(I)))
	-EXP(-MODELb*(T(ILAST)-T(I))))) = E= 0.0;
10	DERIV1(J)~~1000.0*SUM(I,A(I)*T(I)*EXP(ZETA(J)*W(J)*T(I))*
	SIN(WD(J)*T(I))) = E = 0.0;
	DERIV2(J)~~1000.0*SUM(I,A(I)*T(I)*EXP(ZETA(J)*W(J)*T(I))*
	COS(WD(J)*T(I))) = E = 0.0;
	MODEL & MODEL & and MODEL &
15	% MODELAA is the mechanical gain of the system, MODELb, and MODELa
	% are the two time constants of the system in radians. One time constant is
	% associated with the L/R rise time of the motor inductance and the other is
	% the mechanical time constant of the rigid system. The A(I) are the voltages %
	which need to be determined. The T(I) are the times for each of the A(I).
20	% DT is the time spacing of the outputs. W(J) are the undamped flexible
	% modes, WD(J) are the damped flexible modes (in radians/s).

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